

Calculus I

Name: \_\_\_\_\_

Study Guide 26

Class: \_\_\_\_\_

Due Date: \_\_\_\_\_

Score: \_\_\_\_\_

No Work  $\Leftrightarrow$  No Points

Use Pencil Only  $\Leftrightarrow$  Be Neat & Organized

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1. (3 points) State clearly the general comparison property for integration.

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2. (4 points) Use the inequalities  $0 \leq \sin x \leq x$  for  $0 \leq x \leq 1$  to show

$$0 \leq \int_0^1 \sin x^2 dx \leq \frac{1}{3}.$$

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2. \_\_\_\_\_

3. (5 points) Find  $\int_{-2}^4 |x| dx$

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3. \_\_\_\_\_

4. (3 points) State clearly the length of a curve using integration.

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5. (5 points) Find the length of the graph of  $f(x) = \frac{2}{3}\sqrt{x^3}$  for  $0 \leq x \leq 3$ .

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5. \_\_\_\_\_

6. (8 points) Find  $f(1)$  and  $f''(1)$  for  $f(x) = \int_1^{x^2} \frac{1}{1 + \sqrt{t}} dt$ , then discuss its concavity at  $(1, f(1))$ .

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6. \_\_\_\_\_

7. Find the volume of the solid obtained when revolving the enclosed region between the graphs of equations given below by the  $y$ - axis. Drawing Required.

(a) (5 points)  $f(x) = x - 2, x = 0, y = 2$

(b) (5 points)  $f(x) = \sqrt{x}, x = 0, y = 3$

(a) \_\_\_\_\_

(b) \_\_\_\_\_

(c) (6 points)  $f(x) = x^2, g(x) = \sqrt{x}$

(d) (6 points)  $f(x) = \sqrt{5-x}, x = 1, y = 0$

(c) \_\_\_\_\_

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(d) \_\_\_\_\_